

Correcció examen 5

- $\int 4x^3 - 2x^2 + 5x - 1 dx = x^4 - 2\frac{x^3}{3} + 5\frac{x^2}{2} - x + C.$
- $\int (x^4 - \frac{3}{x^5} + x - 8) dx = \int (x^4 - 3x^{-5} + x - 8) dx = \frac{x^5}{5} - 3\frac{x^{-4}}{-4} + \frac{x^2}{2} - 8x + C = \frac{x^5}{5} + \frac{3}{4x^4} + \frac{x^2}{2} - 8x + C.$
- $\int (4x^3 + 8)^5 x^2 dx = \frac{1}{12} \int (4x^3 + 8)^5 12x^2 dx = \frac{(4x^3+8)^6}{72} + C.$
- $\int (2e^x - 3)^{11} e^x dx = \frac{1}{2} \int (2e^x - 3)^{11} 2e^x dx = \frac{(2e^x-3)^{12}}{24} + C.$
- $\int \frac{1}{x\sqrt{\ln x+4}} dx = \int (\ln x + 4)^{-\frac{1}{2}} \frac{1}{x} dx = \frac{(\ln x+4)^{-\frac{1}{2}}}{\frac{1}{2}} = 2\sqrt{\ln x + 4} + C.$
- $\int \frac{3\sin x}{8+2\cos x} dx = 3 \int \frac{\sin x}{8+2\cos x} dx = 3(\frac{-1}{2}) \int \frac{-2\sin x}{8+2\cos x} dx = \frac{-3}{2} \ln(8 + 2\cos x) + C.$
- $\int \frac{e^x}{7+5e^x} dx = \frac{1}{5} \int \frac{5e^x}{7+5e^x} dx = \frac{1}{5} \ln(7 + 5e^x) + C.$
- $\int \operatorname{tag} 2x dx = \int \frac{\sin 2x}{\cos 2x} dx = -\frac{1}{2} \int \frac{-2\sin 2x}{\cos 2x} dx = -\frac{1}{2} \ln(\cos 2x) + C.$
- $\int e^{\cos^2 x} \sin x \cos x dx = \frac{-1}{2} \int e^{\cos^2 x} (-2) \sin x \cos x dx = \frac{-1}{2} e^{\cos^2 x} + C.$
- $\int e^{3x-2} dx = \frac{1}{3} \int e^{3x-2} \cdot 3 dx = \frac{1}{3} \cdot e^{3x-2} + C.$
- $\int \frac{3^x}{2^x} dx = \int (\frac{3}{2})^x dx = \frac{(\frac{3}{2})^x}{\ln(\frac{3}{2})} + C.$
- $\int \frac{4^{2\operatorname{tag} x}}{\cos^2 x} dx = \frac{1}{2} \int \frac{4^{2\operatorname{tag} x}}{\cos^2 x} \cdot 2 dx = \frac{1}{2} \frac{4^{2\operatorname{tag} x}}{\ln 4} + C.$
- $\int \sin(2+3\cos x) \cdot \sin x dx = \frac{-1}{3} \int \sin(2+3\cos x) \cdot (-3) \sin x dx = \frac{-1}{3} \cos(2+3\cos x) + C.$
- $\int \frac{\cos(2\ln x+1)}{x} dx = \frac{1}{2} \int 2 \cdot \frac{\cos(2\ln x+1)}{x} dx = 2 \sin(2\ln x + 1) + C.$
- $\int \frac{x^2}{\cos^2(x^3+2)} dx = \frac{1}{3} \int \frac{3x^2}{\cos^2(x^3+2)} dx = \frac{1}{3} \operatorname{tag}(x^3 + 2) + C.$
- $\int \frac{x dx}{\sqrt{1-x^4}} = \frac{1}{2} \int \frac{2x dx}{\sqrt{1-(x^2)^2}} = \frac{1}{2} \cdot \arcsin(x^2) + C.$
- $\int \frac{1}{x(1+\ln^2 x)} dx = \operatorname{arctag}(\ln x) + C$
- $\int \frac{2 dx}{\sqrt{3-2x^2}} = \frac{2}{\sqrt{3}} \int \frac{1 dx}{\sqrt{1-(\sqrt{\frac{2}{3}}x)^2}} = \frac{2}{\sqrt{3}} \sqrt{\frac{3}{2}} \int \frac{\sqrt{\frac{2}{3}} dx}{\sqrt{1-(\sqrt{\frac{2}{3}}x)^2}} = \frac{2}{\sqrt{2}} \arcsin(\sqrt{\frac{2}{3}}x) + C$
- $\int \frac{5}{2+4x^2} dx = 5 \cdot \frac{1}{2} \int \frac{1}{1+(\sqrt{2}x)^2} dx = \frac{1}{2\sqrt{2}} \cdot \int \frac{\sqrt{2}}{1+(\sqrt{2}x)^2} dx = \frac{1}{2\sqrt{2}} \cdot \operatorname{arctag}(\sqrt{2}x) + C.$

2.- Troba una funció $f(x)$ la derivada de la qual sigui $f'(x)=x^3-1$ i tal que $f(1)=3$.

- $f(x)=\int x^3-1dx = \frac{x^4}{4} - x + C$. Per tant totes les funcions del món tals que $f'(x)=x^3-1$ són de la forma $f(x)=\frac{x^4}{4} - x + C$ i nosaltres en busquem una tal que $f(1)=3$. Per tant $\frac{1^4}{4} - 1 + C = 3 \rightarrow c = 3 + \frac{3}{4} = \frac{15}{4} \rightarrow f(x) = \frac{x^4}{4} - x + \frac{15}{4}$.